

# First-principles calculation of electronic properties of N- and X(X = S, Se, Te)-codoped anatase TiO<sub>2</sub>

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**Abstract:** The impact of N- and X(X = S, Se, Te)-codoping on electronic properties of anatase TiO<sub>2</sub> has been systematically investigated using density functional theory (DFT). The optimized geometry shows that there is large lattice expansion for the codoped anatase TiO<sub>2</sub> due to large atomic radius of the codoped atom. The calculated substitution energies indicate that incorporation of X(X = S, Se, Te) into N-doped bulk TiO<sub>2</sub> can not promote synergistic effect on N after substituting for Ti, whereas it is better after substituting for O. According to the total density of states (DOS) and corresponding partial DOS (PDOS), it can be seen that substituting X(X = S, Se, Te) for O, N 2p orbital is strongly hybridized with impurity states (S 3p, Se 4p, Te 5p). After substituting X(X = S, Se, Te) for Ti, conduction band is mainly dominated by Ti 3d orbit and S 3p (Se 4p or Te 5p)-N 2p-Ti 3d hybridized states are formed. Based on Bader analysis, it can be indicated that the electron transfer is from N to X(X = S, Se, Te) if substituting X(X = S, Se, Te) for O, but it is opposite if substitute X(X = S, Se, Te) for Ti.

**Key words:** anatase TiO<sub>2</sub>; electronic properties; substitution energy; codoping

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TiO<sub>2</sub> (titanium dioxide) has attracted intensive attention due to its extensive applications in decomposition of organic pollutants, solar cells and photo-electrochemical splitting of water<sup>[1,2]</sup>. However, as a wide band gap semiconductor (3.20 eV), anatase allows only absorption of ultraviolet irradiation, which amounts to 3% of solar energy. Only about 5% of the solar spectrum can be utilized due to its wide intrinsic band gap. Furthermore, its photo-excited electron-hole pairs recombine relatively easily. Therefore, it is of great interest to find ways to extend absorption wavelength range of TiO<sub>2</sub> in the visible region without decreasing the photocatalytic activity.

Generally speaking, impurity doping is usually one of the typical approaches to adjust the band gap in the visible region. Research indicates that doping metals and non-metals can obviously narrow the forbidden gap to improve effective photocatalytic performance<sup>[3-9]</sup>. Extensive studies have proposed that N-doped TiO<sub>2</sub> is a promising photocatalytic material<sup>[10,11]</sup>. Umebayashi et al.<sup>[8]</sup> indicated that in the visible region, S-doping caused the absorption edge of TiO<sub>2</sub> to shift into the lower energy region. Theoretical analysis shows that using ab initio calculations, mixing of S 3p states with the valence band contributes to the band gap narrowing. However, S-doped TiO<sub>2</sub> can narrow the band gap, but it is diffi-

cult for S-doped TiO<sub>2</sub> to achieve it due to large formation energies required for substituting S for O in TiO<sub>2</sub><sup>[7]</sup>. So it is important to study the photocatalytic application of S-doped TiO<sub>2</sub>. For the Se-doped study, Jenks et al.<sup>[12]</sup> indicated that the Se-modified TiO<sub>2</sub> displayed greater visible absorption than undoped TiO<sub>2</sub> under ultraviolet (UV) light. Gurkan et al.<sup>[13]</sup> indicated that, for Se(IV)-doped TiO<sub>2</sub>, the experimental results manifested that there is a high visible light absorption from 420 nm to 650 nm. Combined with density functional theory (DFT) calculations, Se(IV)-doped TiO<sub>2</sub> enhances the photocatalytic activity by introducing the additional electronic states originating from the Se 4p orbit in the band gap. However, there is no reported theoretical work focusing on the synergistic effect of Te-doped anatase TiO<sub>2</sub>.

On the basis of DFT for the chalcogen elements mono-doped TiO<sub>2</sub>, there are some researches about N- and X(X = S, Se, Te)-codoped anatase TiO<sub>2</sub>. GAO et al.<sup>[14]</sup> indicated that the experimentally observed absorption edges of (N, S)-codoped TiO<sub>2</sub> are 420, 413, and 429 nm, respectively. DFT calculations explained that N doping leads to the narrowed energy gap with the optical absorption shifting to the red region and S-doping introduces impurity states between the conduction band and the valence

band. Behpour et al.<sup>[15]</sup> confirmed that N and S lead to less grain size, the red shift in optical absorption wavelength to visible region has high photocatalytic activity by different detected measurements. However, there is no reported theoretical work focusing on the synergistic effects of (N,Se)- and (N, Te)-codoped anatase TiO<sub>2</sub> on the mechanism of band-gap narrowing about substituting O and Ti. Our study focuses on the electronic properties of the N-and/or X(X = S, Se, Te)-doped anatase TiO<sub>2</sub> using DFT calculations. In this paper, we try to study the cooperative role of N and X(X = S, Se, Te)-codoped TiO<sub>2</sub> on the mechanism of band-gap reduction of TiO<sub>2</sub>.

## 1 Computational methods and models

All of the spin-polarized calculations were performed using the projector augmented wave (PAW) pseudopotentials for implementation in the Vienna ab initio simulation package (VASP) code<sup>[16,17]</sup>. The Perdew-Burke-Ernzerhof parametrization<sup>[18]</sup> of the generalized gradient approximation<sup>[19]</sup> was adopted for the exchange-correlation potential. The electron wave function was expanded in plane-wave up to the cutoff energy of 420 eV and the optimized lattice constants agreed well with the experimental values. The calculations of optimized geometry and electronic properties were carried out, using the block Davidson scheme<sup>[20,21]</sup> for geometry optimization. The Brillouin-zone integrations were performed using Monkhorst-Pack grids<sup>[22]</sup>. A  $4 \times 4 \times 1$   $k$ -mesh was used for optimization of geometry and a substantially denser  $k$ -mesh of  $8 \times 4 \times 2$  was used for substitution energies, and electronic properties calculations due to  $2 \times 2 \times 2$  anatase supercell was used in this study. The supercell model is shown in Fig. 1.

To overcome the well-known underestimated band gap problem of the metal oxides in 3d electrons, The DFT + U<sup>[23]</sup> approach introduces an on-site correction in order to describe the system with localized d and f electrons, which can produce better band gaps in comparison with experimental results. Here, effective on-site Coulomb interactions  $U$  ( $U = U' - J$ ) for Ti 3d were used to obtain the correct band gap.  $U'$  and  $J$  represent the energy cost of adding an extra electron at a particular site and the screened exchange energy, respectively. Here,  $U = 6.2$  eV was used on Ti 3d electrons. Although the DFT + U approach yields a more accurate band gap, the accuracy in thermodynamic predictions and optimized cell parameters was reduced, owing to dependence on the effective U parameter<sup>[24]</sup>. Therefore, we use DFT + U method for the calculations of structural optimization, substitution energies and

electronic structure.

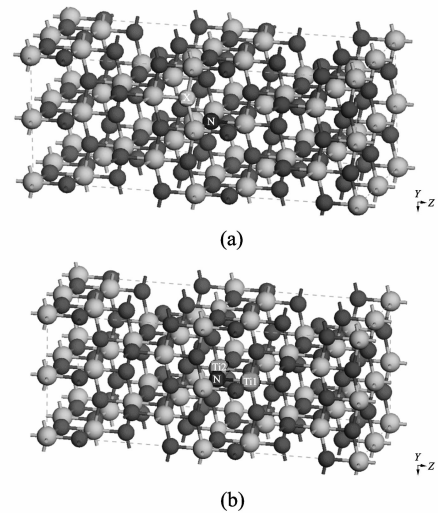


Fig.1 Supercell model for N and X(X = S, Se, Te)-codoped 96-atom anatase TiO<sub>2</sub>, showing the location of the dopants for (a) and (b). The ion doping sites are marked with N, X, Ti1 and Ti2.

## 2 Results and discussion

### 2.1 Geometry analysis

After structural optimization of pure anatase TiO<sub>2</sub>, the optimized lattice parameters are  $a = b = 3.842$  Å,  $c = 9.625$  Å, which are in good agreement with the experimental values,  $a = b = 3.787$  Å,  $c = 9.502$  Å<sup>[25]</sup>, as well as the theoretical results,  $a = b = 3.880$  Å,  $c = 9.681$  Å<sup>[26]</sup>. The result demonstrates that the computational methods adopted in this paper are reasonable and reliable.

The optimized lattice parameters for pure TiO<sub>2</sub>, as well as N- or/and X(X = S, Se, Te)-doped anatase TiO<sub>2</sub> are summarized in Table 1 and Table 2, respectively.

Table 1 Calculated lattice parameters  $a$ ,  $b$ ,  $c$  and  $V$  of pure, N-, S-, Se-, Te-doped and (N, S)-, (N, Se)-, (N, Te)-codoped anatase TiO<sub>2</sub> for substituting O for N and X(X = S, Se, Te). The experimental data and theoretical results are listed for comparison with GGA + U method

	$a(\text{\AA})$	$b(\text{\AA})$	$c(\text{\AA})$	$V(\text{\AA}^3)$
Pure TiO <sub>2</sub> (This work)	7.741	7.741	19.343	1 159.09
Pure TiO <sub>2</sub> ( Experimental <sup>[25]</sup> )	7.564	7.564	19.004	1 087.30
Pure TiO <sub>2</sub> (Theoretical <sup>[26]</sup> )	7.761	7.761	19.362	1 166.23
N-doped TiO <sub>2</sub>	7.746	7.758	19.301	1159.86
S-doped TiO <sub>2</sub>	7.738	7.804	19.331	1 167.35
Se-doped TiO <sub>2</sub>	7.734	7.823	19.337	1 169.95
Te-doped TiO <sub>2</sub>	7.734	7.820	19.461	1 177.00
(N, S)-codoped TiO <sub>2</sub>	7.761	7.752	19.390	1 166.57
(N, Se)-codoped TiO <sub>2</sub>	7.767	7.758	19.406	1 169.34
(N, Te)-codoped TiO <sub>2</sub>	7.775	7.761	19.436	1 172.80

**Table 2** Calculated lattice parameters *a*, *b*, *c* and *V* of pure, N-, S-, Se-, Te-doped and (N, S)-, (N, Se)- and (N, Te)-codoped anatase TiO<sub>2</sub> for substituting Ti for X(X = S, Se, Te) and O for N. The experimental data and other theoretical results are listed for comparison with GGA + U method

	<i>a</i> (Å)	<i>b</i> (Å)	<i>c</i> (Å)	<i>V</i> (Å <sup>3</sup> )
Pure TiO <sub>2</sub> (This work)	7.741	7.741	19.343	1 159.09
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PureTiO <sub>2</sub> (Theoretical <sup>[26]</sup> )	7.761	7.761	19.362	1 166.23
(N, S)1-codoped TiO <sub>2</sub>	7.780	7.785	19.662	1 190.87
(N, S)2-codoped TiO <sub>2</sub>	7.796	7.789	19.685	1 195.33
(N, Se)1-codoped TiO <sub>2</sub>	7.794	7.800	19.666	1 195.56
(N, Se)2-codoped TiO <sub>2</sub>	7.796	7.803	19.651	1 195.41
(N, Te)1-codoped TiO <sub>2</sub>	7.806	7.812	19.715	1 202.23
(N, Te)2-codoped TiO <sub>2</sub>	7.805	7.810	19.723	1 202.26

As seen from Table 1, for mono-doped anatase TiO<sub>2</sub>, the lattice parameters are almost unchanged. Compared with the volume of pure anatase TiO<sub>2</sub> (1 159.09 Å<sup>3</sup>), the volumes of mono-doped anatase TiO<sub>2</sub> are increasing, and the same cases appear in the codoped anatase TiO<sub>2</sub>. It is obvious that the volumes of codoped TiO<sub>2</sub> for replacing O and Ti have different large lattice expansions. By means of calculated data, it is noticed that the supercell has larger lattice expansions due to its larger atomic radius of Se (Se, 1.60 Å; Ti, 1.48 Å) and Te (Te, 1.70 Å; Ti, 1.48 Å), v.s smaller atomic radius of N (0.80 Å), S (1.12 Å) and O (0.60 Å).

## 2.2 Substitution energies

To compare the relative stability of these dopant combinations in anatase TiO<sub>2</sub>, substitution energy (*E*<sub>sub</sub>) of substitutionally doped systems (for either O or Ti) are estimated by

$$E_{\text{sub}} = E_{(\text{doped})} - E_{(\text{pure})} - \mu_{\text{N}} - \mu_{\text{X(X=S, Se, Te)}} + \mu_{\text{O}} + \mu_{\text{Ti}}.$$

where *E*<sub>(doped)</sub> is the total energy of the bulk supercell containing N and X(X = S, Se, Te) atoms, *E*<sub>(pure)</sub> denotes the total energy of pure bulk systems, while  $\mu_{\text{N}}$ ,  $\mu_{\text{X(X=S, Se, Te)}}$ ,  $\mu_{\text{O}}$  and  $\mu_{\text{Ti}}$ , represent the chemical potentials of N, X(X = S, Se, Te), O and Ti atoms, respectively. It should be noticed that the substitution energy depends on the grown conditions, which may be either O- or Ti-rich<sup>[25]</sup>.  $\mu_{\text{O}}$  and  $\mu_{\text{Ti}}$  have the relationship  $\mu_{\text{O}} + \mu_{\text{Ti}} = \mu_{(\text{TiO}_2)}$ . Under Ti-rich condition,  $\mu_{\text{Ti}}$  is considered to be the energy of one atom in the bulk Ti atom ( $\mu_{\text{Ti}} = \mu_{\text{Ti}}^{\text{metal}}$ ) and  $\mu_{\text{O}}$  is calculated by the above formula. Under O-rich grown condition,  $\mu_{\text{O}}$  is estimated by consideration of O<sub>2</sub> molecule and the chemical potential of Ti is taken again as that of one atom in the bulk Ti. The chemical potential  $\mu_{\text{N}}$  is calculated by consideration of one N<sub>2</sub>

molecule ( $\mu_{\text{N}} = \mu_{\text{N}_2}/2$ ) and the chemical potential  $\mu_{\text{X(X=S, Se, Te)}}$  is calculated according to the formula  $\mu_{\text{X(X=S, Se, Te)}} = \mu_{\text{X(X=S, Se, Te)O}_2} - \mu_{\text{O}_2}$ .

As for the so-called substitution energy, it is the energy difference of the system after and before the replacement. The substitution energy indicates that the dopant combinations tend to incorporate into supercell and integrate with each other when both of them are doped in anatase TiO<sub>2</sub>. The calculated results are summarized in Table 3.

**Table 3** Substitution Energy *E*<sub>(sub)</sub> (eV) for N-, S-, Se-, Te-doped, (N, S)-, (N, Se)-, (N, Te)-codoped anatase TiO<sub>2</sub> under Ti-rich and O-rich conditions

Ti-rich		O-rich	
N	5.08	(N, S)1	24.62
S	7.66	(N, S)2	24.51
Se	10.14	(N, Se)1	23.73
Te	13.14	(N, Se)2	23.68
(N, S)	16.69	(N, Te)1	22.36
(N, Se)	16.77	(N, Te)2	22.32
(N, Te)	18.14		

As listed in Table 3, the substitution energies for N- or/and X(X = S, Se, Te)-doped anatase TiO<sub>2</sub> are 5.08, 7.66, 10.14, 13.14, 16.69, 16.77, 18.14 eV under Ti-rich grown condition and 24.62, 24.51, 23.73, 23.68, 22.36 and 22.32 eV under O-rich grown condition, respectively. These suggest that (1) N-doped is easy to incorporate into the anatase TiO<sub>2</sub> under Ti-rich grown condition; (2) With respect to the chalcogen elements substituting O site doped anatase TiO<sub>2</sub>, S is easy, but Te is hard. The same case is to be in the codoped systems; (3) Both N and X(X = S, Se, Te) at the substitutional sites are energetically and preferentially favorable under Ti-rich condition; (4) Under O-rich condition, the incorporation of X(X = S, Se, Te) are gradually decreased, but the case is opposite under Ti-rich condition; (5) The incorporation of X(X = S, Se, Te) can not promote the incorporation of N into bulk TiO<sub>2</sub> under both O- and Ti-rich grown conditions. The (N, Te)-codoped possesses the lowest substitution energy of 22.3 eV among the codoped systems under O-rich grown condition. At the same time, O-rich grown conditions are closest to the experimental environment in conjunction with the sol-gel method for the synthesis of titania. Hence, we will select this configuration to discuss its electronic structure with N- and X(X = S, Se, Te)-codoped compared with N or X(X = S, Se, Te) monodoping. N- and X(X = S, Se, Te)-codoped under Ti-rich condition has the substitutional energy, which is lower than that under O-rich condition. It is a large dif-

ference in the substitution energies obtained by means of DFT + U. The different substitution energies of dopants may be mainly caused by atomic radius.

## 2.3 Electronic structure

The key role to determine the photocatalytic efficiency of anatase  $\text{TiO}_2$  is electronic structure. To understand the origin of band-gap narrowing, two cases about density of states (DOS) and partial DOS

(PDOS) are discussed, as plotted in Figs.2 and 3. For comparison, DOS and PDOS of pure anatase  $\text{TiO}_2$  are also shown in figures, with up-spin DOS above the Fermi level and down-spin DOS below the Fermi level. To modify the band structure of  $\text{TiO}_2$  mono-doping and codoping, the compositions need to be investigated firstly. According to the PDOS of pure  $\text{TiO}_2$ , it can be seen that the valance band edge of  $\text{TiO}_2$  is mainly composed of O 2p states while the conduction band is dominated by Ti 3d states.

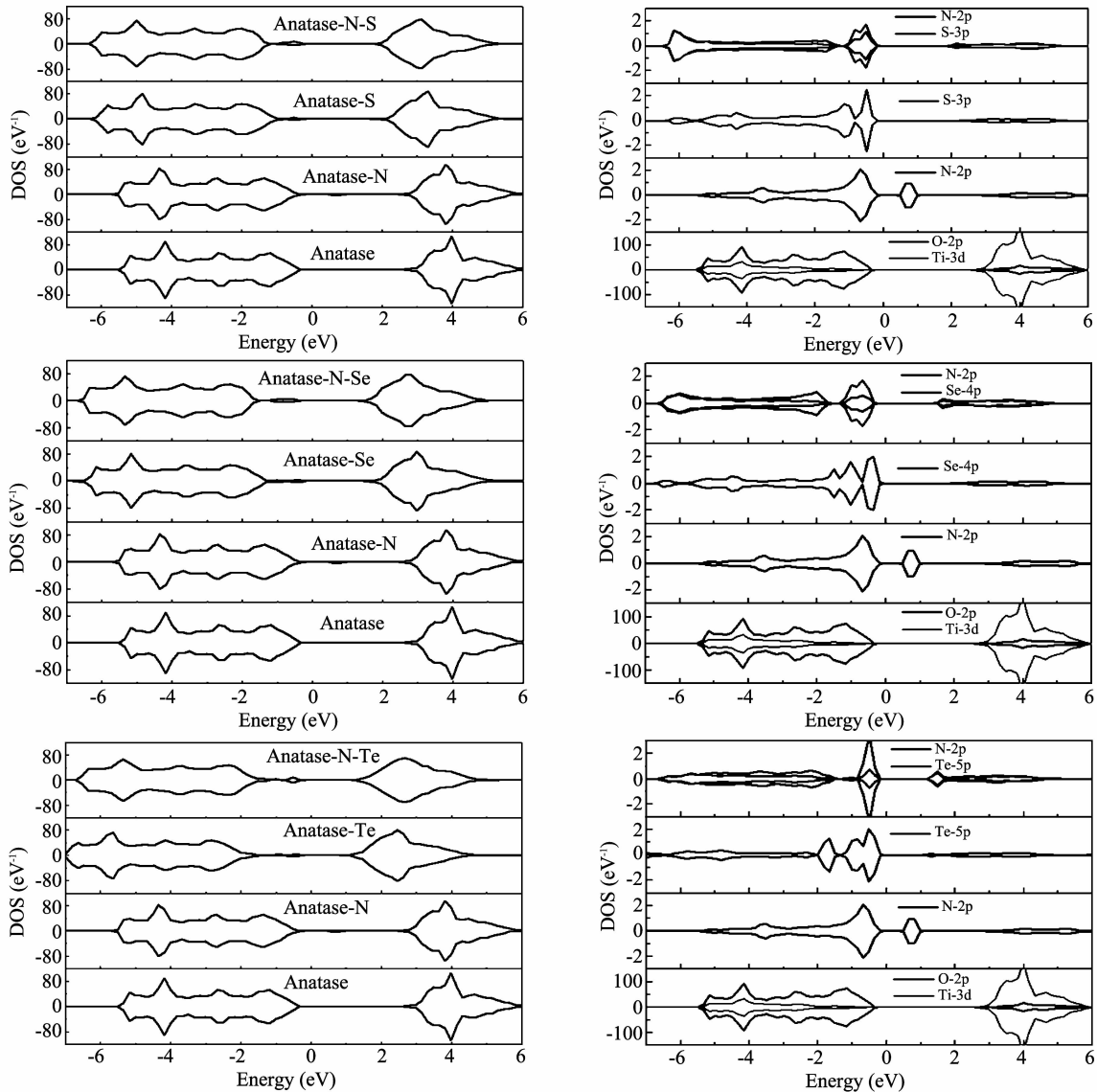


Fig. 2 Calculated DOS and PDOS of pure anatase, N-, S-, Se- and Te-doped, (N, S)-, (N, Se)- and (N, Te)-codoped anatase  $\text{TiO}_2$  for substituting N with X(X= S, Se, Te) for O

For N-doped  $\text{TiO}_2$ , substitution of N at O site, the electronic structures of N and O are  $2s^22p^3$  and  $2s^22p^4$  because N has one electron less than O with respect to p orbital character. In the PDOS of N-doped  $\text{TiO}_2$ , N 2p orbit is mainly located at the top of valance band maximum (VBM) and some states

exist in the conduction band. As shown in the DOS between pure  $\text{TiO}_2$  and N-doped  $\text{TiO}_2$ , from the VBM to the bottom of conduction band (CBM), there is hardly any change in N-doped  $\text{TiO}_2$ . In the case of that, N-doped  $\text{TiO}_2$  is responsible for the photocatalytic activation in the visible-light irradi-

ation. For S-doped  $\text{TiO}_2$ , there are S 3p states localizing slightly above the upper edge of the valence band compared with undoped  $\text{TiO}_2$ . Excitations from the impurity state of S 3p orbit to the conduction band may be responsible for the red shift of the absorption edge observed in S-doped  $\text{TiO}_2$ <sup>[8]</sup>. The width of band gap between VBM and CBM is narrower than that of pure  $\text{TiO}_2$  and N-doped  $\text{TiO}_2$ , which makes the band gap shift to the valance band. For (N, S)-codoped, S 3p orbital is strongly hybridized with N 2p orbit in the valance band. The impurity energy levels at the Fermi level sufficiently overlap with N 2p states located at the VBM of anatase  $\text{TiO}_2$ .

For Se- and Te-doped and (N, Se)-, (N, Te)-codoped  $\text{TiO}_2$ , it is significant from the PDOS that some impurity states below the Fermi level contain

N 2p-Se 4p and N 2p-Te 5p states. The partial Se 4p and Te 5p states are split below the VBM and located at the edge of the conduction band. Incorporations of Se and Te into N-doped anatase  $\text{TiO}_2$  make N 2p orbital character changed, which is fully occupied by N 2p-Se 4p and N 2p-Te 5p states above the VBM. The Se 4p and Te 5p orbital states are maximally dominated in the valance band edge, which makes Se 4p and Te 5p orbital energies vis-à-vis N 2p orbital energy be related to the more delocalized characters of 2p, 4p and 5p states. Therefore, incorporations of N and X (X = S, Se, Te) can modify the CBM and VBM because of their different p orbital energies with respect to N 2p, S 3p, Se 4p and Te 5p orbital states.

Substituting N for O and X (X = S, Se, Te) for Ti, the DOS and PDOS are plotted in Fig. 3.

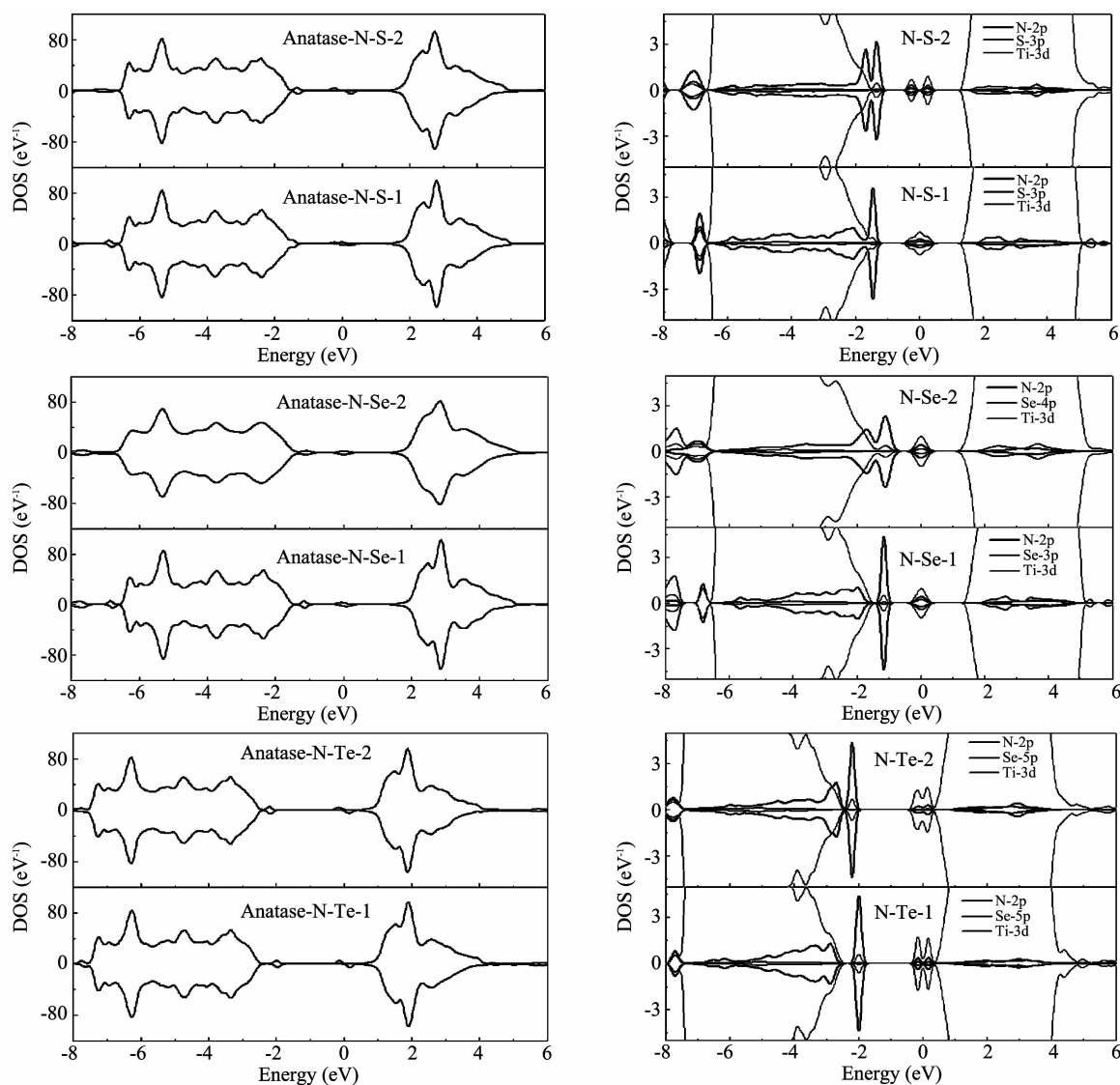


Fig. 3 Calculated DOS and PDOS of pure anatase, N-, S-, Se- and Te-doped, (N, S)-, (N, Se)- and (N, Te)-codoped anatase  $\text{TiO}_2$  for substituting X(X = S, Se, Te) for Ti and N for O

For (N, S)-codoped  $\text{TiO}_2$ , it is found that N 2p states are located above the VBM as well as mixing well with S 3p states. Ti 3d level is dominated by the host CBM while leaving N 2p and S 3p states residing deep in the conduction band. For (N, Se)-codoped case, the conduction band stems mostly from Ti 3d orbital but not from N 2p and Se 4p states. For (N, Te)-codoped, the width of CBM tail is larger than that of (N, S)-, (N, Se)-codoped case. With respect to pure  $\text{TiO}_2$ , the CBM also originates from Ti 3d orbit, whereas S 3p, Se 4p and Te 5p orbits lie in the energy region. For (N, S)2-codoped  $\text{TiO}_2$ , Ti 3d-N 2p-S 3p orbit is split into two parts. In this case, (N, Te)-codoped appears. It is possible that introduction of chalcogen elements into N-doped anatase  $\text{TiO}_2$  leads to large lattice expansion by the large atomic radius. It is evidently found that Ti 3d level is located at the forbidden gap because the strong lattice expansion causes S 3p (Se 4p or Te 5p)-N 2p-Ti 3d hybridized states more significantly, which induces these states to reside in the middle of the gap region. Therefore, it is expected that these states are responsible for large gap narrowing and the hybridization effects may enhance the photocatalytic performance in the visible region.

To investigate the electrons transfer between N and X(X=S, Se, Te), a Bader<sup>[27,28]</sup> analysis of the charge density is performed. The average Bader charges are calculated for N and X(X=S, Se, Te) with respect to substituting N with X(X=S, Se, Te) for O, as plotted in Table 4.

**Table 4** Average Bader charges on dopant atoms and their adjacent atoms in N-, S-, Se-, Te- doped and (N, S)-, (N, Se)- and (N, Te)-codoped anatase  $\text{TiO}_2$  for substituting N with X(X=S, Se, Te) for O

	N	S	Se	Te
N-doped	7.18			
S-doped		6.71		
Se-doped			6.44	
Te-doped				5.97
(N, S)-doped	6.12	6.68		
(N, Se)-doped	6.14		6.41	
(N, Te)-doped	6.19			5.88

The obtained valance electron numbers for N- or X(X=S, Se, Te)- doped anatase  $\text{TiO}_2$  are 7.18, 6.71, 6.44, 5.97, respectively. For N and X(X=S, Se, Te)-codoped anatase  $\text{TiO}_2$ , the electron numbers are 6.12 and 6.68 for (N, S)-codoped, 6.14 and 6.41 for (N, Se)-codoped, 6.19 and 5.88 for (N, Te)-codoped, respectively. It is concluded that there are some changes in the codoped systems. Compared with mono-doped systems, the electron numbers of N are increasing gradually. In (N, S)- and (N, Se)-codoped  $\text{TiO}_2$ , there are 0.56 and 0.27 electrons from S and Se to N, respectively. Howev-

er, in (N, Te)-codoped, there are 0.31 electrons from N to Te.

For replacements of Ti and O with X(X=S, Se, Te) and N, the calculated results are summarized in the Table 5. The obtained valance electron numbers are 6.06 and 4.34 for (N, S)1, 6.05 and 4.30 for (N, S)2, 6.20 and 3.86 for (N, Se)1, 6.19 and 3.88 for (N, Se)2, 6.40 and 3.06 for (N, Te)1, 6.35 and 3.12 for (N, Te)2, respectively. According to the results, it is obviously found that there are about 1.25, 1.28, 1.30, 1.56, 1.13 and 2.02 electrons transfer from the chalcogen elements to N in the (N, S)-, (N, Se)-, (N, Te)-codoped anatase  $\text{TiO}_2$ .

**Table 5** Average Bader charges on dopant atoms and their adjacent atoms in N, S, Se, Te doped and (N, S)-, (N, Se)- and (N, Te)-codoped anatase  $\text{TiO}_2$  for substituting X(X=S, Se, Te) for Ti and N for O

	N	S	Se	Te
(N, S)1-codoped	6.06	4.34		
(N, S)2-codoped	6.05	4.30		
(N, Se)1-codoped	6.20		3.86	
(N, Se)2-codoped	6.19		3.88	
(N, Te)1-codoped	6.40			3.06
(N, Te)2-codoped	6.35			3.12

### 3 Conclusion

The impact of N- and X(X=S, Se, Te)- codoped on the electronic properties of anatase  $\text{TiO}_2$  has been systematically investigated using DFT method. By means of the optimized geometries, it is displayed that the lattice parameters become large expansions because of large atomic radius. According to substitution energies, it is indicated that incorporation of X(X=S, Se, Te) into N-doped bulk  $\text{TiO}_2$  can not promote N synergistic effects for substituting Ti, whereas it is better for substituting O. The PDOS of substitutions of O makes N 2p states be strongly hybridized with impurity states S 3p, Se 4p, Te 5p states. Substituting X(X=S, Se, Te) for Ti atoms, Ti 3d level almost is dominated by the conduction band and forms S 3p (Se 4p or Te 5p)-N 2p-Ti 3d hybrid states. Finally, the Bader analysis demonstrates that the electrons transfer is from N to X(X=S, Se, Te) for chalcogen elements substituting O, however, the substitution of Ti is opposite. Therefore, it is indicated that elemental doping makes the excellent explanation of photocatalytic efficiency in the N- or/and X(X=S, Se, Te)- doped anatase  $\text{TiO}_2$ .

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# N 和硫属元素 X(X = S, Se, Te)共掺杂锐钛矿 $\text{TiO}_2$ 电子性质的第一性原理计算

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**摘 要:** 本文运用密度泛函理论系统地研究了 N 和 X(X = S, Se, Te)共掺杂锐钛矿  $\text{TiO}_2$  时电子特性所受的影响。优化后的结构表明, 在锐钛矿  $\text{TiO}_2$  共掺杂时, 由于掺杂原子有较大的原子半径而引起了大的晶格膨胀。从计算的替换能结果看, 当 X(X = S, Se, Te)掺杂到有 N 原子存在的  $\text{TiO}_2$  时, 若替换 Ti 原子, 则不能很好地促进与 N 的协同作用, 若替换 O 原子, 则相反。从总态密度图和分态密度图来看, 替换 O 原子后的 N 2p 轨道和其他杂质带 S 3p, Se 4p, Te 5p 杂化在一起; 同时替换 Ti 原子后, 导带主要由 Ti 3d 轨道所占据, 从而形成了 S 3p (Se 4p or Te 5p)-N 2p-Ti 3d 杂化态。从 Bader 电荷的结果可知, 替换 O 原子, 电子转移是由 N 到 X(X = S, Se, Te), 而替换 Ti 原子后, 电子转移是由 X(X = S, Se, Te)到 N。

**关键词:** 锐钛矿  $\text{TiO}_2$ ; 电子性质; 替换能; 共掺杂

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